

# Probability distribution table

## Question Paper 2

<b>Level</b>	International A Level
<b>Subject</b>	Maths
<b>Exam Board</b>	CIE
<b>Topic</b>	Discrete random variables
<b>Sub Topic</b>	Probability distribution table
<b>Booklet</b>	Question Paper 2

**Time Allowed:** 59 minutes

**Score:** / 49

**Percentage:** /100

**Grade Boundaries:**

A*	A	B	C	D	E	U
>85%	'77.5%	70%	62.5%	57.5%	45%	<45%

- 1 Ashok has 3 green pens and 7 red pens. His friend Rod takes 3 of these pens at random, without replacement. Draw up a probability distribution table for the number of green pens Rod takes. [4]

- 2 The discrete random variable  $X$  has the following probability distribution.

$x$	-3	0	2	4
$P(X = x)$	$p$	$q$	$r$	0.4

Given that  $E(X) = 2.3$  and  $\text{Var}(X) = 3.01$ , find the values of  $p$ ,  $q$  and  $r$ . [6]

- 3 A team of 4 is to be randomly chosen from 3 boys and 5 girls. The random variable  $X$  is the number of girls in the team.

(i) Draw up a probability distribution table for  $X$ . [4]

(ii) Given that  $E(X) = \frac{5}{2}$ , calculate  $\text{Var}(X)$ . [2]

- 4 The discrete random variable  $X$  takes the values 1, 4, 5, 7 and 9 only. The probability distribution of  $X$  is shown in the table.

$x$	1	4	5	7	9
$P(X = x)$	$4p$	$5p^2$	$1.5p$	$2.5p$	$1.5p$

Find  $p$ . [3]

- 5 In a probability distribution the random variable  $X$  takes the value  $x$  with probability  $kx$ , where  $x$  takes values 1, 2, 3, 4, 5 only.

(i) Draw up a probability distribution table for  $X$ , in terms of  $k$ , and find the value of  $k$ . [3]

(ii) Find  $E(X)$ . [2]

- 6 The probability distribution of the random variable  $X$  is shown in the following table.

$x$	-2	-1	0	1	2	3
$P(X = x)$	0.08	$p$	0.12	0.16	$q$	0.22

The mean of  $X$  is 1.05.

(i) Write down two equations involving  $p$  and  $q$  and hence find the values of  $p$  and  $q$ . [4]

(ii) Find the variance of  $X$ . [2]

- 7 In a particular discrete probability distribution the random variable  $X$  takes the value  $\frac{120}{r}$  with probability  $\frac{r}{45}$ , where  $r$  takes all integer values from 1 to 9 inclusive.

(i) Show that  $P(X = 40) = \frac{1}{15}$ . [2]

(ii) Construct the probability distribution table for  $X$ . [3]

(iii) Which is the modal value of  $X$ ? [1]

(iv) Find the probability that  $X$  lies between 18 and 100. [2]

8 A fair die has one face numbered 1, one face numbered 3, two faces numbered 5 and two faces numbered 6.

(i) Find the probability of obtaining at least 7 odd numbers in 8 throws of the die. [4]

The die is thrown twice. Let  $X$  be the sum of the two scores. The following table shows the possible values of  $X$ .

		Second throw				
		1	3	5	6	6
First throw	1	2	4	6	7	7
	3	4	6	8	9	9
	5	6	8	10	10	11
	5	6	8	10	10	11
	6	7	9	11	11	12
	6	7	9	11	11	12

(ii) Draw up a table showing the probability distribution of  $X$ . [3]

(iii) Calculate  $E(X)$ . [2]

(iv) Find the probability that  $X$  is greater than  $E(X)$ . [2]