

Probability distribution table

Question Paper 4

Level	International A Level
Subject	Maths
Exam Board	CIE
Topic	Discrete random variables
Sub Topic	Probability distribution table
Booklet	Question Paper 4

Time Allowed: 57 minutes

Score: / 47

Percentage: /100

Grade Boundaries:

A*	A	B	C	D	E	U
>85%	'77.5%	70%	62.5%	57.5%	45%	<45%

1 A box contains 5 discs, numbered 1, 2, 4, 6, 7. William takes 3 discs at random, without replacement, and notes the numbers on the discs.

(i) Find the probability that the numbers on the 3 discs are two even numbers and one odd number.

[3]

The smallest of the numbers on the 3 discs taken is denoted by the random variable S .

(ii) By listing all possible selections (126, 246 and so on) draw up the probability distribution table for S . [5]

2 A pet shop has 9 rabbits for sale, 6 of which are white. A random sample of two rabbits is chosen without replacement.

(i) Show that the probability that exactly one of the two rabbits in the sample is white is $\frac{1}{2}$. [2]

(ii) Construct the probability distribution table for the number of white rabbits in the sample. [3]

(iii) Find the expected value of the number of white rabbits in the sample. [1]

- 3 A book club sends 6 paperback and 2 hardback books to Mrs Hunt. She chooses 4 of these books at random to take with her on holiday. The random variable X represents the number of paperback books she chooses.
- (i) Show that the probability that she chooses exactly 2 paperback books is $\frac{3}{14}$. [2]
 - (ii) Draw up the probability distribution table for X . [3]
 - (iii) You are given that $E(X) = 3$. Find $\text{Var}(X)$. [2]
- 4 Coin A is weighted so that the probability of throwing a head is $\frac{2}{3}$. Coin B is weighted so that the probability of throwing a head is $\frac{1}{4}$. Coin A is thrown twice and coin B is thrown once.
- (i) Show that the probability of obtaining exactly 1 head and 2 tails is $\frac{13}{36}$. [3]
 - (ii) Draw up the probability distribution table for the number of heads obtained. [4]
 - (iii) Find the expectation of the number of heads obtained. [2]
- 5 A pet shop has 6 rabbits and 3 hamsters. 5 of these pets are chosen at random. The random variable X represents the number of hamsters chosen.
- (i) Show that the probability that exactly 2 hamsters are chosen is $\frac{10}{21}$. [2]
 - (ii) Draw up the probability distribution table for X . [4]

- 6 Susan has a bag of sweets containing 7 chocolates and 5 toffees. Ahmad has a bag of sweets containing 3 chocolates, 4 toffees and 2 boiled sweets. A sweet is taken at random from Susan's bag and put in Ahmad's bag. A sweet is then taken at random from Ahmad's bag.
- (i) Find the probability that the two sweets taken are a toffee from Susan's bag and a boiled sweet from Ahmad's bag. [2]
- (ii) Given that the sweet taken from Ahmad's bag is a chocolate, find the probability that the sweet taken from Susan's bag was also a chocolate. [4]
- (iii) The random variable X is the number of times a chocolate is taken. State the possible values of X and draw up a table to show the probability distribution of X . [5]