

# Binomial Expansion

## Question Paper 2

<b>Level</b>	International A Level
<b>Subject</b>	Maths
<b>Exam Board</b>	CIE
<b>Topic</b>	Series
<b>Sub Topic</b>	Binomial Expansion
<b>Booklet</b>	Question Paper 2

**Time Allowed:** 63 minutes

**Score:** /52

**Percentage:** /100

**Grade Boundaries:**

A*	A	B	C	D	E	U
>85%	'77.5%	70%	62.5%	57.5%	45%	<45%

- 1 (i) Find the coefficient of  $x^8$  in the expansion of  $(x + 3x^2)^4$ . [1]
- (ii) Find the coefficient of  $x^8$  in the expansion of  $(x + 3x^2)^5$ . [3]
- (iii) Hence find the coefficient of  $x^8$  in the expansion of  $[1 + (x + 3x^2)]^5$ . [4]
- 2 (i) In the expression  $(1 - px)^6$ ,  $p$  is a non-zero constant. Find the first three terms when  $(1 - px)^6$  is expanded in ascending powers of  $x$ . [2]
- (ii) It is given that the coefficient of  $x^2$  in the expansion of  $(1 - x)(1 - px)^6$  is zero. Find the value of  $p$ . [3]
- 3 Find the coefficient of  $x^2$  in the expansion of
- (i)  $\left(2x - \frac{1}{2x}\right)^6$ , [2]
- (ii)  $(1 + x^2)\left(2x - \frac{1}{2x}\right)^6$ . [3]
- 4 (i) Find the first three terms in the expansion of  $(2 + ax)^5$  in ascending powers of  $x$ . [3]
- (ii) Given that the coefficient of  $x^2$  in the expansion of  $(1 + 2x)(2 + ax)^5$  is 240, find the possible values of  $a$ . [3]
- 5 (i) Find the first 3 terms in the expansion of  $(2x - x^2)^6$  in ascending powers of  $x$ . [3]
- (ii) Hence find the coefficient of  $x^8$  in the expansion of  $(2 + x)(2x - x^2)^6$ . [2]
- 6 In the expansion of  $\left(x^2 - \frac{a}{x}\right)^7$ , the coefficient of  $x^5$  is  $-280$ . Find the value of the constant  $a$ . [3]

- 7 Find the coefficient of  $x^3$  in the expansion of  $(2 - \frac{1}{2}x)^7$ . [3]
- 8 Find the coefficient of  $x^6$  in the expansion of  $(2x^3 - \frac{1}{x^2})^7$ . [4]
- 9 The coefficient of  $x^3$  in the expansion of  $(a + x)^5 + (2 - x)^6$  is 90. Find the value of the positive constant  $a$ . [5]
- 10 Find the term independent of  $x$  in the expansion of  $(2x + \frac{1}{x^2})^6$ . [3]
- 11 (i) Find the first 3 terms in the expansion of  $(2 - y)^5$  in ascending powers of  $y$ . [2]
- (ii) Use the result in part (i) to find the coefficient of  $x^2$  in the expansion of  $(2 - (2x - x^2))^5$ . [3]