

# Binomial Expansion

## Question Paper 4

<b>Level</b>	International A Level
<b>Subject</b>	Maths
<b>Exam Board</b>	CIE
<b>Topic</b>	Series
<b>Sub Topic</b>	Binomial Expansion
<b>Booklet</b>	Question Paper 4

**Time Allowed:** 71 minutes

**Score:** /59

**Percentage:** /100

**Grade Boundaries:**

A*	A	B	C	D	E	U
>85%	'77.5%	70%	62.5%	57.5%	45%	<45%

- 1 (i) Find the first 3 terms in the expansion of  $(2 - x)^6$  in ascending powers of  $x$ . [3]
- (ii) Given that the coefficient of  $x^2$  in the expansion of  $(1 + 2x + ax^2)(2 - x)^6$  is 48, find the value of the constant  $a$ . [3]
- 2 (i) Find, in terms of the non-zero constant  $k$ , the first 4 terms in the expansion of  $(k + x)^8$  in ascending powers of  $x$ . [3]
- (ii) Given that the coefficients of  $x^2$  and  $x^3$  in this expansion are equal, find the value of  $k$ . [2]
- 3 (i) Find the first 3 terms in the expansion of  $(2 + 3x)^5$  in ascending powers of  $x$ . [3]
- (ii) Hence find the value of the constant  $a$  for which there is no term in  $x^2$  in the expansion of  $(1 + ax)(2 + 3x)^5$ . [2]
- 4 Find the value of the coefficient of  $x^2$  in the expansion of  $\left(\frac{x}{2} + \frac{2}{x}\right)^6$ . [3]
- 5 (i) Find the first 3 terms in the expansion, in ascending powers of  $x$ , of  $(2 + x^2)^5$ . [3]
- (ii) Hence find the coefficient of  $x^4$  in the expansion of  $(1 + x^2)^2(2 + x^2)^5$ . [3]
- 6 (i) Find the first three terms in the expansion of  $(2 + u)^5$  in ascending powers of  $u$ . [3]
- (ii) Use the substitution  $u = x + x^2$  in your answer to part (i) to find the coefficient of  $x^2$  in the expansion of  $(2 + x + x^2)^5$ . [2]

- 7 Find the coefficient of  $x^2$  in the expansion of  $\left(x + \frac{2}{x}\right)^6$ . [3]
- 8 The first three terms in the expansion of  $(2 + ax)^n$ , in ascending powers of  $x$ , are  $32 - 40x + bx^2$ . Find the values of the constants  $n$ ,  $a$  and  $b$ . [5]
- 9 (i) Find the first 3 terms in the expansion of  $(2 - x)^6$  in ascending powers of  $x$ . [3]  
(ii) Find the value of  $k$  for which there is no term in  $x^2$  in the expansion of  $(1 + kx)(2 - x)^6$ . [2]
- 10 Find the coefficient of  $x$  in the expansion of  $\left(3x - \frac{2}{x}\right)^5$ . [4]
- 11 Find the coefficient of  $x^3$  in the expansion of  
(i)  $(1 + 2x)^6$ , [3]  
(ii)  $(1 - 3x)(1 + 2x)^6$ . [3]
- 12 Find the value of the coefficient of  $\frac{1}{x}$  in the expansion of  $\left(2x - \frac{1}{x}\right)^5$ . [3]
- 13 Find the value of the term which is independent of  $x$  in the expansion of  $\left(x + \frac{3}{x}\right)^4$ . [3]